Effect of Nanoscale Heating on Electrical Transport in RF MEMS Switch Contacts

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I. INTRODUCTION

Many examples of metal contact RF MEMS switches are presented in the literature (for example, [1]–[3]). These have demonstrated the excellent performance typical of MEMS switches—high off-state impedance, low on-state impedance, excellent linearity, and low power consumption. This performance makes them attractive alternatives to solid-state switches in military and commercial radar systems, satellite and wireless communications systems, and wireless sensors [4]. In addition to the advantages mentioned above, metal contact switches offer significantly wider bandwidth as compared to capacitive switches, allowing them to be used in reconfigurable antennas and circuits intended for multiple frequency bands. Understanding the failure of metal contact switches is challenging, however, due to the complex interactions between deformation, current flow, and heating at the contact [5]. Still, individual examples of such switches have demonstrated reliable operation to several billion cycles [3], [6].

Several failure mechanisms have been noted for metal contact switches, including adhesion [3], melting, material transport [7], thermally induced explosions related to boiling of the contact metal [8], and increasing contact resistance [1], [3]. Typically, these failure mechanisms have been noted rather than studied in more depth. For example, an increase in contact resistance as the switch cycles has been reported for both large-scale silver contacts [9] and for MEMS contacts at high cycle numbers [1], [3], but these works have not suggested a hypothesis for the physical cause of the increase.

In addition, it is significant that each failure mechanism above relates to the contact behavior. Therefore, improvements in reliability and power handling capability require a solid understanding of the physics governing contact formation. However, while contact mechanics has been studied extensively over many years, microscale contacts present new challenges. The forces in MEMS contacts (typically tens to hundreds of micro-Newton) are approximately one thousand times smaller than what has previously been considered as a microcontact force—on the order of 200 mN [10]. Such small forces produce contact spots with size normally comparable to or smaller than the electron mean free path in the material (< 50 nm), leading to additional contact resistance due to boundary scattering of electrons passing through the contact.

Heating in contacts due to the passage of current has been studied extensively by Holm [10]. Moreover, finite difference analysis [11] and finite element analysis [12] have both been applied to the heating of contacts in MEMS switches. In all of these works, however, the contact spot size has been assumed to be larger than the electron mean free path. Our experiments suggest that MEMS contacts frequently have spot sizes on the order of or smaller than the mean free path. Such small contact spots are expected to experience reduced heating compared to spots larger than the mean free path.

Hence, in this paper we show that existing contact theory significantly over-predicts contact heating for such small contact spots. We develop improved theory of contact heating for small spots and demonstrate the use of heating for preventing contact resistance increase. In multiple experimental results, we show the accuracy of the improved theory. Further, we investigate the causes of contact resistance increase. The resulting understanding allows improved switch operation by keeping resistance low.

II. EXISTING CONTACT THEORY

A significant component of contact resistance is caused by the roughness of the contacting surfaces (see Fig. 1). As the surfaces come together, high points on each surface make contact, producing real contact at a finite number of asperities. MEMS switch contacts operated under typical conditions are also likely to be covered by a thin insulating film due to process residuals, impurities in the ambient (most likely hydrocarbons), or some...
other source. The presence of this insulating film further limits metal-to-metal contact by allowing real contact only at breaks in the film. This creates a restriction causing a larger resistance across the contact than results from contact asperities alone.

A contact normally consists of multiple spots of different sizes. Therefore, prediction of contact spot size distribution is necessary to fully model contact resistance. Assuming that the spots are sufficiently far apart that they do not interfere significantly with each other, the resistance of the $i$th spot, $r_{ci}$, acts in parallel with the others. Hence, the total contact resistance $R_c$, accounting for $N$ spots, is given by

$$R_c = \left( \sum_{i=1}^{N} r_{ci}^{-1} \right)^{-1}.$$  \hfill (1)

Contact surfaces are often modeled using fractal theory, where the contact spot distribution follows the power law proposed by Mandelbrot [13]. Integrating over each spot gives [14]

$$A_T = \frac{D - 1}{3 - D} A_L$$  \hfill (2)

where $A_T$ is the total contact area, $D$ is the fractal dimension (a parameter between 2 and 3), and $A_L$ is the area of the largest contact spot. AFM imaging of the gold surfaces used for our experiments showed that $D$ for this case is less than 2.05, and therefore $A_T$ is approximately equal to $A_L$—indicating that the largest spot ($i = N_L$), with the lowest contact resistance, dominates the total contact resistance. Then

$$R_c \approx r_c N_L.$$  \hfill (3)

Therefore, the contact resistance can be treated as if it were caused by a single contact spot. By contrast, some previous work in MEMS contacts has estimated that a few tens of asperities were in contact [1], [15]. However, this previous work used a different fabrication process which resulted in much rougher contact dimples, which would cause the assumption that $D$ is near 2 to be violated. Moreover, the estimate that one asperity dominates the resistance does not preclude the presence of additional contact asperities, so long as the additional contact spots are sufficiently smaller than the largest spot to contribute little to the contact conductance.

As current flows, it heats the contact spot to an elevated temperature. This heating can be extremely localized, resulting in contact temperatures tens or even hundreds of degrees higher than the surrounding material. For metal contacts, Holm has expressed the contact spot temperature $T_c$ as a function of contact voltage $V_c$ as [10]

$$T_c = \sqrt{\frac{V_c^2}{4L} + T_0^2}.$$  \hfill (4)

Here, $L = 2.45 \times 10^{-8} \text{ W} \cdot \text{m} / \text{K}^2$ is the Lorenz constant and $T_0$ is the ambient temperature. At sufficient contact temperature, annealing of the contact takes place, reducing the contact hardness (a phenomenon known as “contact softening” [10]). Moreover, heating of the contact spot may also cause breakdown or delamination of the insulating film, allowing real contact over a larger area. Either effect is measured as a decrease in contact resistance. This is illustrated in Fig. 1. The published softening temperature for gold contacts is 100°C, corresponding to a contact voltage of 70–80 mV for contacts near room temperature [10]. Contact melting or boiling (see Fig. 2) is also possible at higher temperatures. For gold these occur at 1063 and 2817°C, respectively, or about 430 and 900 mV, according to (4).

III. FABRICATION AND EXPERIMENTS

To study contact heating and its effects on contact resistance, we fabricated and tested metal-contact MEMS switches. A SEM
image of a typical switch is shown in Fig. 3. The switch consists of a fixed-fixed beam situated across the ground lines of a coplanar waveguide. The beam and underlying electrodes are sputtered gold. Electrostatic force is used to pull the beam down until the dimple in the center of the beam contacts the central conductor of the waveguide. To avoid charging, there is no dielectric film coating the actuation electrodes. Instead, the stiffness of the beam is relied upon to prevent shorting. The total gap under the beam is 1.54 μm, with a dimple height of 1.18 μm, leaving a distance of 0.36 μm to travel before contact occurs. The tested beams had a width of 100 μm, a thickness of 3.1 μm, and a length of either 400 or 500 μm. The beam geometry allows four-point probe measurements of contact resistance, as illustrated in Fig. 3. The dimples varied in size between 5 × 5 and 20 × 20 μm, but no difference in contact resistance behavior was seen between dimples of varying size. SEM imaging of the dimples suggests that the bottoms are very flat, without any detectable curvature, as shown in Fig. 4(a). Similarly, AFM imaging of the contact electrode showed that it has rms roughness of approximately 13 nm. A sample AFM scan is shown in Fig. 4(b).

We measured switch pull-down voltage (the voltage just required to initiate contact) and ultimate pull-in voltage (the voltage causing unstable collapse onto the actuation electrodes) and compared them to predictions of a mechanical model to extract Young’s modulus and residual stress. We estimated the Young’s modulus of our gold film to be 50 ± 5 GPa, with a residual tensile stress of about 92 ± 6 MPa. Several papers have previously reported estimates between 50–55 GPa for Young’s modulus of microfabricated gold structures, comparing well with our measurement [16]–[18]. Contact occurred at approximately 55 V for the 500 μm beam and about 60 V for the 400 μm beam, and catastrophic collapse onto the actuation electrodes occurs at about 100 and 124 V, respectively.

The contact force in the switches was calculated based on the measured actuation voltage using a mechanical-electrostatic model employing the finite difference method to simulate mechanical deflection. A reduced-order model based on relations for the capacitance of a microstrip line was used to simulate the electrostatic force [19]. The model was validated by comparison to simulations using both ANSYS and CoventorWare.
Both comparisons showed a maximum error in the contact force of less than 1.4% over a variety of loading conditions. However, the uncertainty in the values of Young’s modulus and residual stress contributes to uncertainty in the contact force predictions. Overall, we estimate that the contact forces reported here are accurate to within ±10 μN up to a contact force of about 218 μN [20]. Using this same technique, we estimate contact opening forces (or elastic restoring forces) of 60 and 70 μN for the 500 and 400 μm beams, respectively.

A. Fabrication

The switches were fabricated using metal surface micromachining, shown in Fig. 5. The substrate is a silicon wafer with a layer of thermal oxide for isolation. The first gold layer, used for actuation and contact electrodes and for wiring, is sputtered and patterned, Fig. 5(a). Next, a thin layer of photoresist is spun on and patterned to define the anchors, Fig. 5(b). The thickness of this layer determines the gap between the dimple and the contact electrode. The second layer of photoresist is then spun on and patterned to define the dimples, Fig. 5(c). Finally, the mechanical layer of gold is sputtered and patterned to create the beams, Fig. 5(d). In the end, the beams are released by wet etching and supercritical drying, Fig. 5(e).

B. Experimental Setup

To avoid stiction, the switches were tested in a sealed vacuum chamber kept at 5–8 mTorr. An illustration of the experimental setup is shown in Fig. 6. The vacuum level is sufficient to reduce the moisture in the chamber, but not to ensure a clean gold surface, and thus a thin hydrocarbon layer probably coats the gold surface [21]. Nevertheless, at low moisture, the switches showed significantly reduced adhesion. When operated in air, the switches sometimes stuck down, but those operated in vacuum did not. The chamber is also fitted with a temperature controller that operates from room temperature to over 700 K.

Contact resistance has been shown both experimentally and numerically to remain equal to its dc value at extremely high frequencies (for these switches, higher than 20 THz) [22], [23]. Hence, our experiments were simplified by measuring the dc contact resistance rather than S-parameters. Two multimeters were used to record current flow and voltage drop across the contact using the four-point probe technique. A dual-channel power supply was used to provide the contact voltage as well as the actuation signal, with a voltage amplifier to provide the high actuation voltage. All instruments were controlled by a computer running LabVIEW. The contact force was controlled by varying the actuation voltage. We found that after fabrication, the switches normally showed very high contact resistance (above 100 kΩ). However, by applying a burn-in contact voltage of 2–3 V, the resistance was reduced to 1–2 Ω. The burn-in process is very similar to A-fritting as discussed by Holm [10]. It is unknown, however, whether the same physics is involved. After burn-in, 500 cold-switched break-in cycles were performed.

The power supply (Agilent E3646A) allows both a current limit and a voltage limit to be set. When the output is turned on, the instrument increases the voltage until either limit is reached, allowing for operation in either current-controlled or voltage-controlled modes. Hence, we were able to specify either the contact voltage or the contact current. For example, when applying the 2–3 V burn-in signal mentioned above, we set the current limit to 1 mA, so that the power supply automatically reduced the voltage when the contact resistance dropped, preventing contact melting. Similarly, during the 500 break-in cycles, the power supply provided 5 mA of current through the contact in each break-in cycle.

IV. EXPERIMENTAL RESULTS

First, we tested the response of the contact resistance to externally applied heating. As subsequent results will show, we were able to increase the resistance in a switch by mechanical cycling without the application of current to the contact. Using this method, we raised the resistance in a switch to about 68 Ω. Using the thermal stage, we then raised the temperature of the entire
chip from room temperature to 90 °C and recorded the contact resistance during heating. The results are shown in Fig. 7. The stage was heated at a rate of 6 °C per minute, sufficiently slow to assume quasistatic heating of the contact. The contact voltage was maintained below 10 mV to prevent self-heating, and the contact force was approximately 80 μN. During heating, we observed a large drop in contact resistance, from about 70 Ω to about 3 Ω. In fact, the resistance began to drop soon after the temperature began to rise, but the largest portion of the drop occurred between 60 and 70 °C.

A resistance reduction caused by contact heating is called “contact softening” [10], [24]. Note, however, that true contact softening occurs in surfaces heated sufficiently to cause annealing of dislocations in the contact. Since our contacts contain impurities, it is uncertain whether the observed resistance reduction is due to annealing or to enhanced diffusion of the impurities away from the contact at elevated temperature, resulting in a larger contact area. However, since both effects are caused by heating, we will refer to any thermally induced resistance reduction as contact softening. This paper will further explore the cause of the resistance reduction after presenting all of the relevant data.

We can approximate the softening temperature (or temperature causing softening) as ∼ 65 °C, significantly smaller than the published softening temperature of 100 °C, which is based on the assumption of contact annealing. Note that thermal stress during heating will increase the contact force somewhat (predicted contact force at 90 °C is about 218 μN). However, tests performed at room temperature show that varying contact force by changing actuation voltage causes a 4% drop in contact resistance between 80 and 218 μN—much less than the dramatic 95% decrease seen here. Similarly, several previous results for microscale contact resistance have shown little dependence on contact force for forces between about 100 and 1,000 μN [11], [25], [26]. Hence, the majority of the resistance drop is caused by the externally applied heating.

Next, we studied self-heating of the contact. We measured V–I curves of the contact resistance under varying contact force (that is, using different actuation voltages) for hundreds of contact events on more than 10 switches. The data were taken by stepping the current and measuring the contact voltage. At least 50 cycles separated each V–I test to prevent any test being affected by the previous ones. We found that an increase in contact voltage beyond a threshold caused the contact resistance to decrease in every case. After the decrease, the contact resistance remained low for immediately subsequent cycles. However, during the 50 cycles after each V–I curve, the contact resistance returned to its original value. Fig. 8 shows typical voltage-contact resistance curves for a 500 μm beam at six levels of contact force. The raw V–I data are shown in the inset. The resistance remains nearly constant or shows a slight rise (due to the increase in resistivity with temperature) until the voltage reaches approximately 70–80 mV. At this point, the resistance decreases rapidly, similar to experimental data in [10] or [27].

A. Low-Resistance Switch Operation

Experiments also revealed that with switches tested using a low voltage limit of 10 mV, the contact resistance tended to continuously increase as the switch cycled. The cause of this resistance increase is not known, but it has been observed previously [1], [3]. We will present a hypothesis for this resistance increase in the next section. However, we found that when the voltage limit was increased above 0.5 V (while keeping the current below 1 mA to avoid excessive heating), contact heating caused the contact resistance to stay nearly constant over hundreds of cycles. We observed this behavior under both hot and cold switching. Here, hot switching is defined as switching performed with a voltage placed across the contacts throughout the on–off cycle. In cold switching, voltage is only placed on the switch when the electrodes are in contact. Typical cold-switched results are shown for the both steady resistance and rising resistance in Fig. 9(a) and (b). The contact force in each cycle for this data is about 48 μN.

To demonstrate that the elevated temperature resulting from contact heating is responsible for avoiding the contact resistance rise, we tested a switch heated to 80 °C using externally-applied heating from the thermal stage. The current and voltage limits, and the contact force, were the same as the data in Fig. 9(b)—1 mA, 10 mV, and 48 μN (note that in this experiment
Fig. 9. Cold-switched operation with current limit of 1 mA and voltage limit of (a) 1.3 V (showing steady resistance) and (b) 0.01 V (showing rising resistance).

Fig. 10. Comparison of contact resistance for contacts operated at room-temperature and heated to 80 °C.

the actuation voltage was reduced to keep the contact force the same at elevated temperature). Fig. 10 compares the resulting contact resistance measurements to the data in Fig. 9(b). Over more than 200 cycles, while the room-temperature contact resistance increases hundreds of times, the heated contact resistance remains low, showing that heating prevents the increase in contact resistance. While these low-cycle experiments cannot prove that life may be extended in this way, these results suggest that contact heating may be used to avoid this important failure mechanism for MEMS switches.

TABLE I

<table>
<thead>
<tr>
<th>Average Contact Resistance Increase After…</th>
<th>(Ohms)</th>
<th>Std. Dev.</th>
</tr>
</thead>
<tbody>
<tr>
<td>14 days with no operation</td>
<td>5.24</td>
<td>±0.222</td>
</tr>
<tr>
<td>19 days with no operation</td>
<td>7.88</td>
<td>±0.814</td>
</tr>
<tr>
<td>100 cycles with ( V_c = 10 ) mV</td>
<td>33.6</td>
<td>±11.7</td>
</tr>
<tr>
<td>100 cycles with ( V_c = 0 )</td>
<td>36.1</td>
<td>±7.32</td>
</tr>
</tbody>
</table>

B. Exploration of Resistance Increase

Table I summarizes experimental results that give a better understanding of contact resistance rise. The first two lines give the average resistance rise after no operation for 14 and 19 days, respectively. In this case, the contact resistance of a switch was measured (~2 Ω), and the contact was then opened. For the next two weeks, neither it nor any of the switches nearby was tested, while the chip remained in the vacuum chamber. On the fourteenth day, the switch was cycled five times with a contact force of about 48 μN. The average contact resistance was 5.24 Ω higher than the initial contact resistance, with a standard deviation of 0.2 Ω. After five further days of no additional operation, the switch was cycled another five times at the same contact force. In these cycles, the average contact resistance showed an overall increase of 7.88 Ω (with standard deviation of 0.8 Ω) compared to the initial contact resistance of 2 Ω. Hence, although the process was quite slow, the contact resistance increased even when no handling of the switches took place. The most likely cause for such an increase is the gradual build-up or repair of an insulating film.

The last two lines compare the average contact resistance rise after 100 cycles for switches tested with a voltage limit of 10 mV and for switches tested with no contact voltage applied. These experiments were performed to test the hypothesis that electrostatic force pulled impurities into the contact area, increasing resistance. In each case, three sets of 100 cycles were averaged, with each set beginning after the contact was softened to an initial resistance of 5–10 Ω. As before, the contact force in each case was about 48 μN. The results indicate a statistically insignificant difference. Hence, mechanical cycling alone is an important factor in the resistance increase.

C. Inconsistencies With Existing Contact Heating Theory

The data in Fig. 8 indicate contact resistance reduction at a threshold voltage of approximately 75–80 mV for an initial contact resistance near 1 Ω. This threshold voltage is called the “softening voltage” [10], [24]. (Initial contact resistance here is the resistance measured at the start, on the linear part of the \( V-I \) curve.) However, further testing showed that the softening voltage increases as the contact resistance rises. This was tested by measuring \( V-I \) curves with a variety of initial contact resistance magnitudes. Fig. 11 gives the softening voltages extracted from \( V-I \) curves of 21 contacts with initial contact resistances varying from 0.5 to 336 Ω. The resistances were varied by using mechanical cycling to raise the resistance and contact heating to reduce it. The plot shows that the softening voltage increases for larger initial contact resistance from about 70 mV at 0.5 Ω.
to over 350 mV at 336 °C (again, a contact force of about 48 μN was used). These values are all higher than predictions using existing theory, as shown by the line at 52 mV. This line represents the voltage prediction from (4) for heating a contact from 22 to 65 °C, the softening temperature measured from Fig. 7. In fact, existing theory gives no explanation for why contact heating should depend on the initial contact resistance. To explain these inconsistencies, we develop below improved theory for modeling the contact heating in MEMS-scale contacts. First, we consider further the cause of the resistance increase.

V. DISCUSSION OF RESULTS

While Fig. 10 shows that contact heating prevents immediate contact resistance rise, the cause of this rapid rise was not apparent. We had previously suggested that cold-working of the contact asperities led to hardening of the metal, increasing contact resistance [28]. However, while this may be responsible for a portion of the observed increase, it is unlikely that strain hardening can account for a thousand-fold increase like that shown in Fig. 9(b). Since contact resistance scales as the square root of hardness [24], such a large increase in resistance would require hardness to increase one million times.

In fact, only the presence of impurities is likely to cause such a large change in contact resistance. We have already mentioned that previous work indicated that sputtered gold films most likely retain a thin insulating layer, probably composed of hydrocarbons adsorbed onto the surface [21]. The high contact resistance of the switches prior to burn-in supports this idea. However, we believe that actual metal-to-metal contact occurs after the initial burn-in because the V-I curves are very linear up to the softening voltage, as will be shown in Fig. 15. In addition, we have found that contacts with lower contact resistance have higher adhesion, suggesting that a larger metal area is in contact [29].

The results reported in Table I further support the idea that the resistance increase is caused by build-up of an insulating film, with mechanical cycling largely responsible for the build-up. The contact behavior suggested by our results is summarized in Fig. 12. Part (a) shows two surfaces in contact. Both surfaces are covered with an insulating film. Placing sufficient voltage on the contact surfaces causes breakdown of the insulating film, allowing current flow, Fig. 12(b). When the surfaces pull apart, the contact spot is still bare (no film), as depicted in Fig. 12(c). However, randomness in the contact closing process causes the film-free spots to be misaligned in subsequent cycles, Fig. 12(d). This causes the insulating film to be pressed onto the edges of the film-free areas, promoting regrowth of the film and leading to increasing contact resistance. This behavior also explains why there appears to be just one real contact spot. When the insulating film initially breaks down in one spot, the voltage immediately drops as current begins to flow, reducing the stress on the rest of the film. Based on this hypothesis, the contact resistance increase would not be observed in ultra-high vacuum, since it has been shown that the film is removed in such an environment [21].

VI. THEORY

For a contact radius on the order of the electron mean free path (about 38 nm in gold [30]) or smaller, the current is constricted by both lattice scattering and boundary scattering of electrons. For both ohmic constriction and boundary scattering, the contact resistance \( R_c \) for a spot of radius \( a \) is [31]

\[
R_c = \gamma \left( \frac{\lambda}{a} \right) R_M + R_S = \frac{1}{1 + 0.83 \left( \frac{\lambda}{a} \right) 2a} + 4\rho \frac{\lambda}{3\pi a^2} \quad \text{(5)}
\]

where \( \lambda \) is the mean free path, and \( \rho \) is the electrical resistivity. \( R_M \) is the Maxwell spreading resistance (the resistance due to lattice scattering), and \( R_S \) is the Sharvin resistance (the additional resistance due to boundary scattering in small constricitions). Also, \( \gamma(\lambda/a) \) is a scaling function. While this equation is well-known, most of the existing work on contact heating considers only the contribution of the Maxwell spreading resistance [10], [32]. Even for the smallest contact resistance in Fig. 11 of 0.5 Ω, (5) gives a contact radius of 51.8 nm, comparable to the electron mean free path. (For this calculation, we used a measured resistivity of \( 3.6 \times 10^{-8} \, \Omega \cdot \text{m} \).) Hence, much of the measured resistance results from boundary scattering of electrons. However, boundary-scattered electrons do...
not transfer heat to the metal lattice within the contact constriction (see [33]), leading to a reduction in the contact temperature for a given contact voltage. The existing model of contact heating does not include this effect.

In addition, the existing model of (4) assumes that the temperature far from the contact spot is equal in each of the contacting bodies. This is not true for many MEMS contacts, since the small size of the moving contact makes heating of the entire moving body unlikely. Hence, a difference exists between the substrate (at room temperature) and the moving body (at an elevated temperature). Therefore, understanding of the nanoscale contact heating requires consideration of both the device-level temperature and the extremely localized heating of the contact spot. At the nanometer scale, models relate the real contact size and contact voltage with the contact temperature. On the device level, an integrated electrothermal model is necessary to describe the relationship between current flow and temperature.

### A. Asperity Heating Model

The goal of the nanoscale contact heating model is to relate the contact voltage $V_c$ to the contact spot temperature $T_c$ while considering the effects of contact spot size. The principle difference between the theory presented here and existing theory is that we assume that heating in the contact is due only to the Maxwell term in (5), $\gamma R_M$.

Greenwood and Williamson have previously shown that equipotential surfaces are also isothermals in a contact [32]. For initial development of the model, we assume that the contact is symmetric, with maximum temperature at the contact asperity. This assumption will be relaxed later. Hence, we analyze a half-contact. See Fig. 13 for an illustration, with labels showing potential, resistance, and temperature at the contact spot, an arbitrary intermediate isothermal-equipotential surface, and on a surface sufficiently far from the contact. We further assume that the potential $\phi$ on an equipotential surface can be broken into Maxwell and Sharvin components as

$$\phi = \phi_M + \phi_S = I(R_{eM} + R_{eS}).$$

(6)

$R_{eM}$ and $R_{eS}$ are the Maxwell and Sharvin components of resistance between the surface and the contact spot, and $R_e = R_{eM} + R_{eS}$ is the total resistance in the same volume.

Assuming that the Maxwell resistance is the only source of contact heating, we can write the total heat generated between the contact spot and any isothermal as $I\phi_M$. The isothermal differential temperature is then

$$dT = -I\phi_M dR_e$$

(7)

where $dR_e$ is the corresponding differential thermal resistance of the surface. If we assume that conduction through the metal is the dominant form of heat transfer through the contact, we can also compare the differential thermal and electrical resistances on any equipotential surface via the relation

$$dR_e = \frac{d\phi}{\rho_e \kappa_e} = \frac{d\phi}{I \rho_e \kappa_e}.$$  

(8)

Here, $\rho_e$ and $\kappa_e$ are the effective electrical resistivity and thermal conductivity of the metal accounting for size effects. Substituting (6) and (8) into (7) then gives

$$dT = \frac{I R_{eM}}{\rho_e \kappa_e} d\phi = -\frac{R_{eM} \phi}{R_e \kappa_e} d\phi.$$  

(9)

Integrating from the contact spot to the far surface produces

$$\int_{T_c}^{T_0} \rho_e \kappa_e dT = \frac{\gamma R_M V_c^2}{8 R_e}.\,$$

(10)

Unfortunately, the detailed geometry of the contact is required to calculate $R_e$ and $R_{eM}$. However, we may estimate the ratio $R_{eM}/R_e$ as that of the overall Maxwell resistance to the overall contact resistance, $R_{eM}/R_e \approx \gamma R_M/R_e$. Making this substitution into (10) and evaluating the integral gives

$$\int_{T_c}^{T_0} \frac{\rho_e \kappa_e dT}{\rho_e \kappa_e} = \frac{\gamma R_M V_c^2}{8 R_e}.\,$$

(11)

The left-hand side of (11) may be evaluated using the Wiedemann–Franz law. This law states that for metals, $\rho_e = LT$, where $\rho$ and $\kappa$ are the material electrical resistivity and thermal conductivity [34]. The Wiedemann–Franz law has been shown to apply even at atomicist length scales, the size of the smallest possible contact spots, so it applies to the factor $\rho_e \kappa_e$ as well [35], resulting in

$$L(T_c^2 - T_0^2) = \frac{\gamma R_M V_c^2}{4 R_e}.\,$$

(12)

The only difference between (12) and (4) is the factor $\gamma R_M/R_e$. This factor is nearly unity when $R_e$ is small (when $a$ is much larger than $\lambda$), and it decreases to nearly zero for large $R_e$ (when $a$ is much smaller than $\lambda$). Therefore, for a small contact resistance, (12) is equal to (4), deviating only when boundary scattering contributes to the contact resistance.

Equation (12) gives the asperity temperature assuming both contact surfaces are at the same temperature $T_0$. As described above, the moving surface in a MEMS switch is likely to be heated by the passage of current, and so the material in the contact surfaces is at different temperatures $T_2$ and $T_1$ (we arbitrarily choose $T_2 > T_1$). In this case, a constant additional heat.

[Image: Fig. 13. Half of a contact showing the contact surface, an intermediate isothermal-equipotential surface, and a surface far from the contact spot. Labels show the potential and resistance (measured with respect to the contact surface) as well as temperature.]
flux $\dot{q}$ will flow through the contact, and so (7) will have an additional term

$$dT = (-I \phi_M \pm \dot{q}) dr_e.$$  

(13)

The flux $\dot{q}$ is added if the isothermal surface is in contact body 1 (at $T_1$) and subtracted in body 2 (at $T_2$). Following the same derivation used for (12) leads to

$$L (T_c^2 - T_{f2}^2) = \frac{\gamma R_M}{4 R_e} V_c^2 + \frac{\dot{q}}{I} V_c$$  

(14)

$$L (T_c^2 - T_{f2}^2) = \frac{\gamma R_M}{4 R_e} V_c^2 - \frac{\dot{q}}{I} V_c.$$  

(15)

Eliminating $\dot{q} V_c / I$ from both equations yields

$$T_c^2 = \frac{\gamma R_M}{4 R_e} L V_c^2 + \frac{1}{2} (T_1^2 + T_2^2).$$  

(16)

We remark that (16) is identical to (12) when $T_1 = T_2 = T_0$. We also note that (12) has been experimentally validated using MEMS switch contacts [36].

B. Electrothermal Model

Use of (16) requires knowledge of $T_1$ and $T_2$, the temperatures of the contacting bodies. We can assume that the fixed contact remains at ambient temperature, $T_1 \approx T_0$. However, electrothermal modeling of the switch is required to calculate $T_2$, the temperature in the moving contact. The electrothermal model used here is described in [37]. Briefly, 2-D finite element modeling (FEM) is used to solve the heat equation with the electric current as a heat source. The model includes effects due to heat conduction and contact heating, as well as electrical and thermal contact resistance. Convective and radiative heat transfer are ignored because they are insignificant.

C. Comparison to Experimental Data

Using the combination of FEM and (16), we analyzed the data of Fig. 8 to determine the contact spot temperature and percent real contact area increase. First, we used the FEM to calculate the temperature in the beam near the contact. We then computed the contact spot temperature using (16). Finding the real contact area requires knowledge of the change in average electrical resistivity as the contact is heated. Holm estimated that the average resistivity changes as [10]

$$\rho = \rho_0 + \frac{2L \Delta T}{3k}$$  

(17)

where $\rho$ and $\rho_0$ are respectively the average and room temperature resistivities and $\Delta T = T_c - T_0$, the difference between the contact spot temperature and room temperature. We estimated the contact spot size for each data point of Fig. 8 using (5) and (17), allowing estimation of the area increase as $a^2 / a_0^2$, where $a$ is the real contact radius and $a_0$ is the initial contact radius (the first data point for each $V-I$ curve).

Fig. 14 shows the calculated percent contact area increase as a function of the predicted contact temperature. The data show rapidly increasing contact area about above 65 °C. This result agrees well with the experimental threshold temperature of 60–70 °C. However, we emphasize again that these temperatures are well below the published softening temperature for gold of 100 °C [10]. We believe that the resistance decrease in our experiments is due to the thermal breakdown of bonds between the gold and the insulating film, allowing the film to be easily pushed aside. Alternatively, it has been shown that gold melting temperature drops for small gold particles [38]. Hence, it is also possible that softening occurs at reduced temperature for small contact spots. Softening at the published softening temperature has been linked to annealing, leading to a reduction in hardness of the work-hardened contact spot [10]. We believe that the reason for the disparity is that our measurements are recording a different physical phenomenon (breakdown of an insulating film) that seems to dominate contact resistance in low-force MEMS contacts.

Four $V-I$ curves from the tests summarized in Fig. 11 are shown in Fig. 15 and compared to model predictions of asperity temperature. The contacts had initial resistance of 2, 17, 50, and 336 Ω. Contact temperature isothermals are shown for temperatures from 30 to 100 °C. These isothermal lines were calculated.
We performed experiments that demonstrated a contact resistance reduction when a metal-to-metal contact is heated. This reduction is called contact softening. Softening occurs both for externally-heated contacts and for those heated by the passage of current (see Figs. 7 and 8). We also found that existing theory over-predicts internal heating for MEMS contacts. In addition, we showed that contacts with larger resistance require a higher contact voltage for heating. This effect is not predicted by existing theory (see Fig. 11). Therefore, we proposed a new approach to explain these effects. The resulting theory predicts that for a given contact voltage, small contact spots with a radius less than about 40 nm (those with high resistance) will show reduced heating compared to larger spots. This is because boundary-scattered electrons (which account for much of the resistance of small spots) do not heat the contact region. Our predictions compare well with experimental data. Using the theory to explain experimental results, we can confirm that both externally-heated and voltage-heated contacts are softened at a temperature of 60–70 °C. Further, as shown in Fig. 15, increasing the contact current after softening takes place leads to further resistance reduction. This further reduction occurs such that the contact temperature remains nearly constant despite the increased current (see the shaded region in Fig. 15). This allows approximate prediction of the contact resistance after the contact has been softened at a given current.

We also found that contact heating can be used to control contact resistance increase, a commonly-reported failure mechanism for MEMS switches. Our experiments showed that unheated contacts showed significantly larger resistance as the switch cycled. The data suggest that this increase may be due to the build-up of an insulating film. However, contacts heated either externally or internally (by the passage of current) showed low resistance over many hundreds of cycles (see Figs. 9 and 10). Further experiments are planned to study the effect of contact heating on switch lifetime. We believe that heating breaks down the insulating film, reducing resistance. Therefore, contact heating allows control of contact resistance in MEMS switches. Comparisons between theory and experiments verify this conclusion.

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